

Coreference Resolution

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Coreference resolution (CR) vs. Anaphora resolution (AR)

1/3

AR \subset CR???

- There are people thinking that $AR \subset CR$
- “*Every speaker has to present his paper*”
 - “his” needs “every speaker” to be understood
 - “his” and “every speaker” are not coreferentOtherwise :
“Every speaker had to present every speaker’s paper”

*Exemples de (Sukthanker et al., 2018)

Coreference resolution (CR) vs. Anaphora resolution (AR)

2/3

CR \subset AR???

- There are also people thinking that CR \subset AR
- *“If he is unhappy with your work, the CEO will fire you”*
 - **“he”** and **“CEO”** are coreferent
 - **“he”** appears before **“CEO”** (*cataphore*)

*Exemples de (Sukthanker et al., 2018)

Coreference resolution (CR) vs. Anaphora resolution (AR)

3/3

In order to be clear

- Coreference : implies that two mentions refer (clearly) to the same entity
- Anaphore : a mention needs an antecedent in order to be understandable
-> there is not necessarily coreference

*Exemples de (Sukthanker et al., 2018)

Coreference types 1/2

- **Zero anaphora**

“You always have **[two fears]** : **[your commitment]** versus **[your fear]**”

- **One anaphora**

“Since Samantha has set her eyes on **[the beautiful villa by the beach]**, she just wants to buy **[that one]**”

- **Demonstratives**

“**[This car]** is much more spacious and classy than **[that]**”

- **Presuppositions**

“If there is **[anyone]** who can break the spell, it is **[you]**”

*Exemples de (Sukthanker et al., 2018)

Non-anaphoric pronouns

- **Clefts**

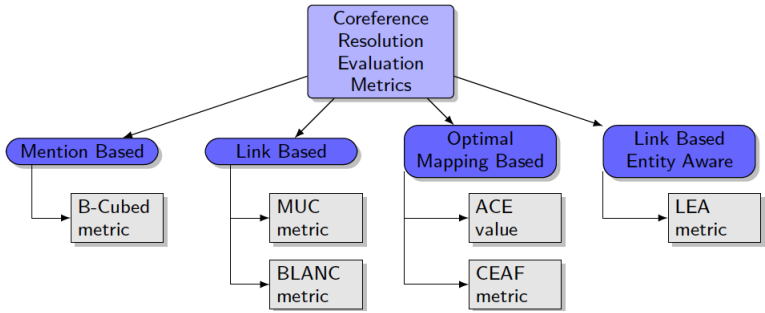
“**[It]** was Tabby who drank the milk.”

- **Pleonastic “It”**

“**[It]**'s raining man !”

*Exemples de (Sukthanker et al., 2018)

Evaluation metrics overview



(Sukthanker et al., 2018)

Data for coreference resolution

Today there are “enough” (?) :

- French : ANCOR, Democrat
- English : MUC 6 et 7, Semeval 2011 et 2012
- Several other languages : (Nedoluzhko et al., 2022)
CorefUD 1.0 : Coreference Meets Universal Dependencies

Semeval 2012 corpus

- Version 5 Ontonotes corpus (Pradhan et al., 2012)
→ News data
- In 3 languages (English the most used)
- Annotationtype : coreferences (no non-coreferent anaphora)
→ Annotation of singletons
- The most used corpus

Approche (Soon et al., 2001) (2)

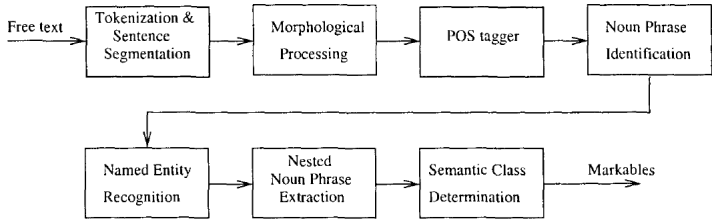


Figure – Processing pipeline (Soon et al., 2001)

- Phase 1 : repérage des mentions (*markables*)
- bout-en-bout (!!!)
- 85% des mentions repérées

Approche (Soon et al., 2001) (6)

Algorithme d'apprentissage :
arbres de décision (C5 (Quinlan 1993))

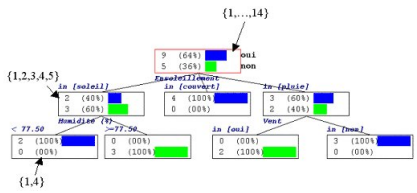


Figure – Exemple d'arbre de décision (Wikipedia)

Approche (*Soon et al., 2001*) (7)

Évaluation

- Données : *MUC-6* et *MUC-7* (articles de *news*)
20910 exemples (6,5% positifs) et 48872 exemples (4,4%), respectivement
- Résultats :
 - *MUC-6* : P=67.3, R=58.6, F1=62.6
 - *MUC-7* : P=65.5, R=56.1, F1=60.4

Approche (Ng and Cardie, 2002) (2)

Caractéristiques

Feature Type	Feature	Description
Lexical	SOON_STR	C if, after discarding determiners, the string denoting NP _i matches that of NP _j ; else I.
Grammatical	PRONOUN_1*	Y if NP _i is a pronoun; else N.
	PRONOUN_2*	Y if NP _j is a pronoun; else N.
	DEFINITE_2	Y if NP _j starts with the word "the;" else N.
	DEMONSTRATIVE_2	Y if NP _j starts with a demonstrative such as "this," "that," "these," or "those;" else N.
	NUMBER*	C if the NP pair agree in number; I if they disagree; NA if number information for one or both NPs cannot be determined.
	GENDER*	C if the NP pair agree in gender; I if they disagree; NA if gender information for one or both NPs cannot be determined.
	BOTH_PROPER_NOUNS*	C if both NPs are proper names; NA if exactly one NP is a proper name; else I.
Semantic	APPOSITIVE*	C if the NPs are in an appositive relationship; else I.
	WNCLASS*	C if the NPs have the same WordNet semantic class; I if they don't; NA if the semantic class information for one or both NPs cannot be determined.
	ALIAS*	C if one NP is an alias of the other; else I.
Positional	SENTNUM*	Distance between the NPs in terms of the number of sentences.

Approche (Ng and Cardie, 2002) (4)

Résultats

System Variation	C4.5						RIPPER					
	MUC-6			MUC-7			MUC-6			MUC-7		
	R	P	F	R	P	F	R	P	F	R	P	F
Original Soon et al.	58.6	67.3	62.6	56.1	65.5	60.4	-	-	-	-	-	-
Duplicated Soon Baseline	62.4	70.7	66.3	55.2	68.5	61.2	60.8	68.4	64.3	54.0	69.5	60.8
Learning Framework	62.4	73.5	67.5	56.3	71.5	63.0	60.8	75.3	67.2	55.3	73.8	63.2
String Match	60.4	74.4	66.7	54.3	72.1	62.0	58.5	74.9	65.7	48.9	73.2	58.6
Training Instance Selection	61.9	70.3	65.8	55.2	68.3	61.1	61.3	70.4	65.5	54.2	68.8	60.6
Clustering	62.4	70.8	66.3	56.5	69.6	62.3	60.5	68.4	64.2	55.6	70.7	62.2
All Features	70.3	58.3	63.8	65.5	58.2	61.6	67.0	62.2	64.5	61.9	60.6	61.2
Pronouns only	-	66.3	-	-	62.1	-	-	71.3	-	-	62.0	-
Proper Nouns only	-	84.2	-	-	77.7	-	-	85.5	-	-	75.9	-
Common Nouns only	-	40.1	-	-	45.2	-	-	43.7	-	-	48.0	-
Hand-selected Features	64.1	74.9	69.1	57.4	70.8	63.4	64.2	78.0	70.4	55.7	72.8	63.1
Pronouns only	-	67.4	-	-	54.4	-	-	77.0	-	-	60.8	-
Proper Nouns only	-	93.3	-	-	86.6	-	-	95.2	-	-	88.7	-
Common Nouns only	-	63.0	-	-	64.8	-	-	62.8	-	-	63.5	-

Résultats de (Soon et al., 2001) :

- MUC-6 : P=67.3, R=58.6, F1=62.6

- MUC-7 : P=65.5, R=56.1, F1=60.4

Approche (*Fernandes et al., 2012*) (1)

Article : *Latent Structure Perceptron with Feature Induction for Unrestricted Coreference Resolution*

Auteurs : Fernandes, Dos Santos et Milidiù

- Représentation des entités (ou *clusters*) avec des arbres
- Apprentissage de structures latentes avec le *perceptron* structuré
- Optimisation d'une fonction de coût incluant l'information des entités
- Déduction automatique de caractéristiques complexes par entropie
- Évaluation sur les données de la campagne *CoNLL Eval 2012*

Approche (*Fernandes et al., 2012*) (2)

Approche en 2 étapes :

- 1 Détection des mentions dans le texte
⇒ approche par analyse syntaxique (groupes nominaux et pronoms) + entités nommées
(dos Santos and Carvalho, 2011)
- 2 *Clusterisation* des mentions
⇒ perceptron structuré

Approche (*Fernandes et al., 2012*) (3)

Large margin structure perceptron :

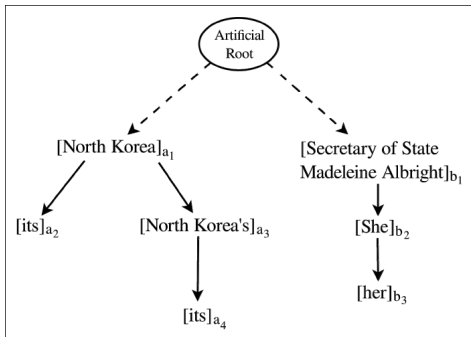
$$F^\ell(\mathbf{x}) = \arg \max_{y' \in \mathcal{Y}(\mathbf{x})} s(\mathbf{y}'; \mathbf{w}) + \ell(\mathbf{y}, \mathbf{y}')$$

$$s(\mathbf{y}'; \mathbf{w}) = \mathbf{w}^T \phi(\mathbf{x}, \mathbf{y}')$$

Approche (Fernandes et al., 2012) (4)

Structures latentes : arbres de coréférences

North Korea_{a₁} opened **its**_{a₂} doors to the U.S. today, welcoming **Secretary of State Madeleine Albright**_{b₁}. **She**_{b₂} says **her**_{b₃} visit is a good start. The U.S. remains concerned about **North Korea's**_{a₃} missile development program and **its**_{a₄} exports of missiles to Iran.



Approche (Fernandes et al., 2012) (5)

Apprentissage des structures latentes

$$F(\mathbf{x}) \equiv F_y(F_h(\mathbf{x}))$$

```

 $\mathbf{w}_0 \leftarrow \mathbf{0}$ 
 $t \leftarrow 0$ 
while no convergence
  for each  $(\mathbf{x}, \mathbf{y}) \in \mathcal{D}$ 
     $\tilde{\mathbf{h}} \leftarrow \arg \max_{\mathbf{h} \in \mathcal{H}(\mathbf{x}, \mathbf{y})} \langle \mathbf{w}_t, \Phi(\mathbf{x}, \mathbf{h}) \rangle$ 
     $\hat{\mathbf{h}} \leftarrow \arg \max_{\mathbf{h} \in \mathcal{H}(\mathbf{x})} \langle \mathbf{w}_t, \Phi(\mathbf{x}, \mathbf{h}) \rangle + \ell_r(\mathbf{h}, \tilde{\mathbf{h}})$ 
     $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + \Phi(\mathbf{x}, \tilde{\mathbf{h}}) - \Phi(\mathbf{x}, \hat{\mathbf{h}})$ 
     $t \leftarrow t + 1$ 
 $\mathbf{w} \leftarrow \frac{1}{t} \sum_{i=1}^t \mathbf{w}_i$ 

```

$\mathcal{H}(x)$ feasible document trees for x

$\Phi(x, h)$ feature vector representation of x and h

Approche (*Fernandes et al., 2012*) (6)

$\phi(\mathbf{x}, \mathbf{y})$ utilise 70 caractéristiques de base de 4 types :

- Lexical
- Syntaxique
- Sémantique
- Distance et position

+ les caractéristiques complexes déduites automatiquement par entropie

⇒ e.g. 196 caractéristiques au total pour l'anglais

Approche (*Fernandes et al., 2012*) (7)

Résultats

Language	MUC			B ³			CEAF _e			Mean
	R	P	F ₁	R	P	F ₁	R	P	F ₁	
Arabic	43.63	49.69	46.46	62.70	72.19	67.11	52.49	46.09	49.08	54.22
Chinese	52.69	70.58	60.34	62.99	80.57	70.70	53.75	37.88	44.44	58.49
English	65.83	75.91	70.51	65.79	77.69	71.24	55.00	43.17	48.37	63.37
									Official Score	58.69

Approche (*Durrett and Klein, 2013*) (1)

Article : *Easy Victories and Uphill Battles in Coreference Resolution*

Auteurs : Durrett and Klein

- Même type de modèle que le précédent (Fernandes et al., 2012) (weighted features)
- Patrons des caractéristiques extraits automatiquement (et non pas par heuristique)
- Caractéristiques assez génériques (et pas beaucoup)
- Système état-de-l'art
- Analyse très intéressante des “succès” (*easy victories*) et des erreurs (*uphill battles*)

Approche (*Durrett and Klein, 2013*) (2)

- Détection de mentions : texte annoté avec analyse syntaxique et entités nommées
- 3 types de mentions :
 - pronoms
 - noms propres (entités nommées)
 - groupes nominaux (analyse syntaxique)

Approche (*Durrett and Klein, 2013*) (3)

Modèle de coréférence : modèle log-linéaire

$$P(a|x) \propto \exp\left(\sum_{i=1}^n \mathbf{w}^\top \mathbf{f}(i, a_i, x)\right)$$

Avec :

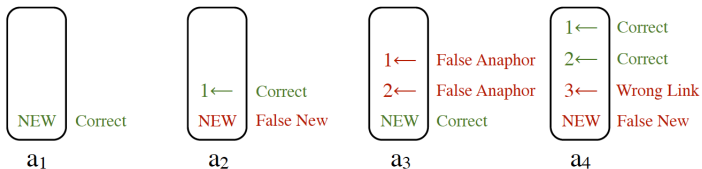
- x ensemble des mentions dans un document
- $a = (a_1, \dots, a_N)$ un *clustering* particulier où $a_i = j$ implique que l'antécédent de la mention i est la mention j
- f *feature functions*
- w les paramètres du modèle (à apprendre)

Approche (Durrett and Klein, 2013) (4)

Apprentissage du modèle :

$$\ell(\mathbf{w}) = \sum_{k=1}^t \log \left(\sum_{a \in \mathcal{A}(C_k^*)} P'(a|x_k) \right) + \lambda \|\mathbf{w}\|_1$$

$$l(a, C^*) = \alpha_{\text{FA}} \text{FA}(a, C^*) + \alpha_{\text{FN}} \text{FN}(a, C^*) + \alpha_{\text{WL}} \text{WL}(a, C^*)$$



[Voters]₁ agree when [they]₁ are given a [chance]₂ to decide if [they]₁ ...

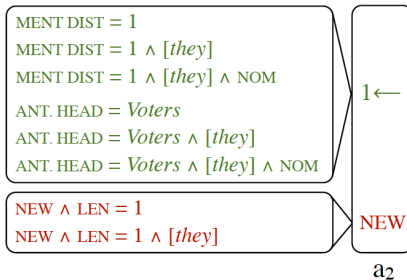
Approche (*Durrett and Klein, 2013*) (5)

Caractéristiques :

Feature name	Count
Features on the current mention	
[ANAPHORIC] + [HEAD WORD]	41371
[ANAPHORIC] + [FIRST WORD]	18991
[ANAPHORIC] + [LAST WORD]	19184
[ANAPHORIC] + [PRECEDING WORD]	54605
[ANAPHORIC] + [FOLLOWING WORD]	57239
[ANAPHORIC] + [LENGTH]	4304
Features on the antecedent	
[ANTECEDENT HEAD WORD]	57383
[ANTECEDENT FIRST WORD]	24239
[ANTECEDENT LAST WORD]	23819
[ANTECEDENT PRECEDING WORD]	53421
[ANTECEDENT FOLLOWING WORD]	55718
[ANTECEDENT LENGTH]	4620
Features on the pair	
[EXACT STRING MATCH (T/F)]	47
[HEAD MATCH (T/F)]	46
[SENTENCE DISTANCE, CAPPED AT 10]	2037
[MENTION DISTANCE, CAPPED AT 10]	1680

Approche (*Durrett and Klein, 2013*) (6)

Caractéristiques “conjointes” :



[*Voters*]₁ generally agree when [*they*]₁ ...

Approche (*Durrett and Klein, 2013*) (7)

Easy victories :

	MUC	B^3	CEAF _e	Avg.
STANFORD	60.46	65.48	47.07	57.67
IMS	62.15	65.57	46.66	58.13
SURFACE	64.39	66.78	49.00	60.06

Système état-de-l'art malgré l'ensemble (restreint) de caractéristiques !

Approche (*Durrett and Klein, 2013*) (8)

Analyse : même résultat avec caractéristiques automatiques et heuristiques !

	MUC	B^3	CEAF _e	Avg.
SURFACE	64.39	66.78	49.00	60.06
-1STWORD	63.32	66.22	47.89	59.14
+DEF-1STWORD	63.79	66.46	48.35	59.53
-PRONCONJ	59.97	63.46	47.94	57.12
+AGR-PRONCONJ	63.54	66.10	48.72	59.45
-CONTEXT	60.88	64.66	47.60	57.71
+POSN-CONTEXT	62.45	65.44	48.08	58.65
+DEF+AGR+POSN	64.55	66.93	48.94	60.14

Erreurs :

	Nominal/Proper				Pronominal	
	1 st w/head		2 nd + w/head			
Singleton	99.7%	18.1K	85.5%	7.3K	66.5%	1.7K
Starts Entity	98.7%	2.1K	78.9%	0.7K	48.5%	0.3K
Anaphoric	7.9%	0.9K	75.5%	3.9K	72.0%	4.4K

Approche (*Durrett and Klein, 2013*) (9)

Uphill battles : caractéristiques

- Hyperonymie et synonymie depuis *WordNet*
- Nombre et genre des mentions
- Entités nommées
- *Clusters* latents (e.g. *president*, *leader* ...)

Approche (Clark and Manning, 2015) (2)

2 modèles locaux sur paires de mentions :

- modèle de classification
- modèle de *ranking*

Les 2 sous forme de modèle "logistique" :

$$p_{\theta}(a, m) = (1 + e^{\theta^T f(a,m)})^{-1}$$

Mêmes caractéristiques, paramètres (θ_c, θ_r) et fonction de coût différents

Approche (*Clark and Manning, 2015*) (3)

Modèles locaux sur paires de mentions, fonctions de coût :
- classificateur

$$\mathcal{L}_c(\theta_c) = - \sum_{m \in \mathcal{M}} \left(\sum_{t \in \mathcal{T}(m)} \log p_{\theta_c}(t, m) \right. \\ \left. + \sum_{f \in \mathcal{F}(m)} \log(1 - p_{\theta_c}(f, m)) \right) + \lambda \|\theta_c\|_1$$

- modèle de *ranking*

$$\mathcal{L}_r(\theta_r) = - \sum_{m \in \mathcal{M}} \left(\max_{t \in \mathcal{T}(m)} \log p_{\theta_r}(t, m) \right. \\ \left. + \min_{f \in \mathcal{F}(m)} \log(1 - p_{\theta_r}(f, m)) \right) + \lambda \|\theta_r\|_1$$

\mathcal{M} ensemble de toutes les mentions

$\mathcal{T}(m)$ mentions coréférentes avec m

$\mathcal{F}(m)$ mentions non coréférentes avec m

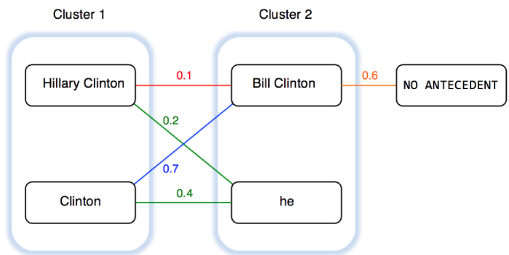
Approche (*Clark and Manning, 2015*) (4)

Caractéristiques :

- Distance
- Syntaxiques
- Sémantiques
- À base de règles
- Lexicales
- Caractéristiques conjointes (Durrett and Klein, 2013)

Approche (*Clark and Manning, 2015*) (5)

Modèle de *clustering* (*Entity-Centric*), exemple :



- Between Clusters Features:**
- Max-Prob = 0.7
 - Min-Prob = 0.1
 - Avg-Prob = 0.35
 - Avg-Prob_non-pronoun_pronoun = 0.3
 - ⋮
- Other Features:**
- Second-Cluster-Not-Anaphoric = 0.6
 - Document-Size = 132
 - ⋮

Approche (Clark and Manning, 2015) (7)

Résultats : comparaison avec l'état-de-l'art

	MUC			B ³			CEAF _{φ₄}			CoNLL
	Prec.	Rec.	F ₁	Prec.	Rec.	F ₁	Prec.	Rec.	F ₁	Avg. F ₁
Fernandes et al.	75.91	65.83	70.51	65.19	51.55	57.58	57.28	50.82	53.86	60.65
Chang et al.	-	-	69.48	-	-	57.44	-	-	53.07	60.00
Björkelund & Kuhn	74.3	67.46	70.72	62.71	54.96	58.58	59.4	52.27	55.61	61.63
Ma et al.	81.03	66.16	72.84	66.90	51.10	57.94	68.75	44.34	53.91	61.56
Durrett & Klein (INDEP.)	72.27	69.30	70.75	60.92	55.73	58.21	55.33	54.14	54.73	61.23
Durrett & Klein (JOINT)	72.61	69.91	71.24	61.18	56.43	58.71	56.17	54.23	55.18	61.71
This work	76.12	69.38	72.59	65.64	56.01	60.44	59.44	52.98	56.02	63.02

Approche (*Wiseman et al., 2016*) (1)

Article : *Learning Global Features for Coreference Resolution*

Auteurs : Wiseman, Rush et Shieber

- Modèle local : *mention ranking* ...
- ... mais guidé par une information globale :
une représentation (vectorielle) des clusters !
- première approche dans son genre
- approche état-de-l'art (évidemment !)

Approche (Wiseman et al., 2016) (2)

Motivations de la méthode :

DA: um and [I]₁ think that is what's - Go ahead [Linda]₂.

LW: Well and uh thanks goes to [you]₁ and to [the media]₃ to help [us]₄...So [our]₄ hat is off to all of [you]₅ as well.

Approche (Wiseman et al., 2016) (4)

Calcul des représentation des mentions (pour les clusters) :

$$h_c(x_n) \triangleq \tanh(W_c \phi_a(x_n) + b_c)$$

Avec :

- $\phi_a(x_n)$ vecteur creux ($\{0, 1\}^F$) représentant des caractéristiques discrètes
- W_c, b_c paramètres (à apprendre)

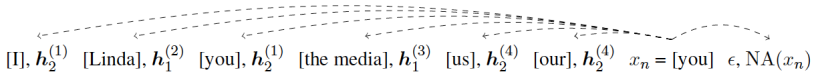
Approche (Wiseman et al., 2016) (5)

Calcul des représentation des clusters :

$$h_j^{(m)} \leftarrow \text{RNN}(h_c(X_j^{(m)}), h_{j-1}^{(m)}; \theta)$$

DA: um and [I]₁ think that is what's - Go ahead [Linda]₂.

LW: Well and thanks goes to [you]₁ and to [the media]₃ to help [us]₄...So [our]₄ hat is off to all of [you]₅...



Approche (Wiseman et al., 2016) (6)

Calcul des représentation des clusters :



Approche (Wiseman et al., 2016) (9)

Apprentissage :

$$\sum_{n=1}^N \max_{\hat{y} \in \mathcal{Y}(x_n)} \Delta(x_n, \hat{y})(1 + f(x_n, \hat{y}) + g(x_n, \hat{y}, \mathbf{z}^{(o)}) - f(x_n, y_n^\ell) - g(x_n, y_n^\ell, \mathbf{z}^{(o)})),$$

$$y_n^\ell \triangleq \arg \max_{y \in \mathcal{Y}(x_n): z_y^{(o)} = z_n^{(o)}} f(x_n, y) + g(x_n, y, \mathbf{z}^{(o)})$$

Approche (Wiseman et al., 2016) (11)

Résultats :

System	MUC			B ³			CEAF _e			CoNLL
	P	R	F ₁	P	R	F ₁	P	R	F ₁	
B&K (2014)	74.3	67.46	70.72	62.71	54.96	58.58	59.4	52.27	55.61	61.63
M&S (2015)	76.72	68.13	72.17	66.12	54.22	59.58	59.47	52.33	55.67	62.47
C&M (2015)	76.12	69.38	72.59	65.64	56.01	60.44	59.44	52.98	56.02	63.02
Peng et al. (2015)	-	-	72.22	-	-	60.50	-	-	56.37	63.03
Wiseman et al. (2015)	76.23	69.31	72.60	66.07	55.83	60.52	59.41	54.88	57.05	63.39
This work	77.49	69.75	73.42	66.83	56.95	61.50	62.14	53.85	57.70	64.21

Approche “Kenton Lee”

Article : *End-to-end Neural Coreference Resolution*
Auteurs : Lee, He, Lewis et Zettlemoyer

- Caractéristiques
- Premier système neuronal bout-à-bout (*end-to-end*)
 - Il se passe de l’annotation *gold* des mentions
 - Il résolve implicitement le problème des enchâssements

Approche “Kenton Lee” (suite...)

Le modèle

- $$P(y_1, \dots, y_N | D) = \prod_{i=1}^N P(y_i | D) = \prod_{i=1}^N \frac{\exp(s(i, y_i))}{\sum_{y' \in \mathcal{Y}(i)} \exp(s(i, y'))}$$

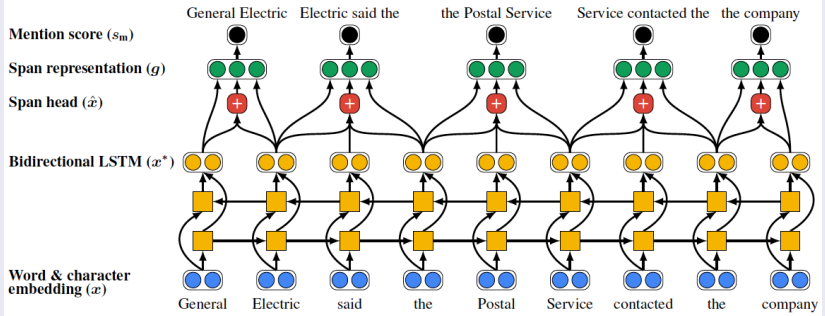


$$s(i, j) = \begin{cases} 0 & j = \epsilon \\ s_m(i) + s_m(j) + s_a(i, j) & j \neq \epsilon \end{cases}$$

- $s_m(i) = w_m \cdot \text{FFNN}(g_i)$
- $s_a(i, j) = w_a \cdot \text{FFNN}(g_i, g_j, g_i \odot g_j, \phi(i, j))$
- g_i sont les représentations des mentions de mots
- $\phi(i, j)$ encode orateur, genre, distance entre les mentions

Approche "Kenton Lee" (suite...)

Architecture neuronale



*Image de (Lee et al. 2017)

Approche “Kenton Lee” : évaluation 1/3

Résultats globaux

	MUC			B ³			CEAF _{ϕ_4}			Avg. F1
	Prec.	Rec.	F1	Prec.	Rec.	F1	Prec.	Rec.	F1	
Our model (ensemble)	81.2	73.6	77.2	72.3	61.7	66.6	65.2	60.2	62.6	68.8
Our model (single)	78.4	73.4	75.8	68.6	61.8	65.0	62.7	59.0	60.8	67.2
Clark and Manning (2016a)	79.2	70.4	74.6	69.9	58.0	63.4	63.5	55.5	59.2	65.7
Clark and Manning (2016b)	79.9	69.3	74.2	71.0	56.5	63.0	63.8	54.3	58.7	65.3
Wiseman et al. (2016)	77.5	69.8	73.4	66.8	57.0	61.5	62.1	53.9	57.7	64.2
Wiseman et al. (2015)	76.2	69.3	72.6	66.2	55.8	60.5	59.4	54.9	57.1	63.4
Clark and Manning (2015)	76.1	69.4	72.6	65.6	56.0	60.4	59.4	53.0	56.0	63.0
Martschat and Strube (2015)	76.7	68.1	72.2	66.1	54.2	59.6	59.5	52.3	55.7	62.5
Durrett and Klein (2014)	72.6	69.9	71.2	61.2	56.4	58.7	56.2	54.2	55.2	61.7
Björkelund and Kuhn (2014)	74.3	67.5	70.7	62.7	55.0	58.6	59.4	52.3	55.6	61.6
Durrett and Klein (2013)	72.9	65.9	69.2	63.6	52.5	57.5	54.3	54.4	54.3	60.3

